Bottomonium in thermal medium from NRQCD on $N_f = 2 + 1$ light flavor lattices

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Outline









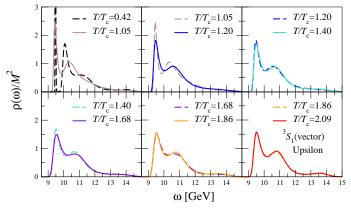


study how bottomonium behaves

in thermal medium

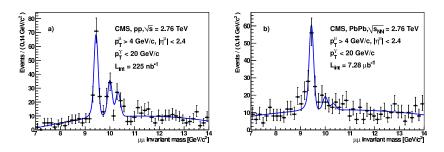
(around the deconfinement temperature)

T-dependence of the Υ spectral function



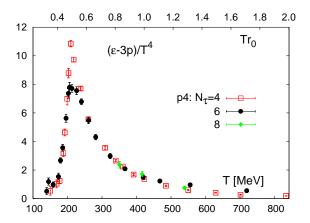
G. Aarts et al, PRL106 (2011) 061602, JHEP1111 (2011) 103

CMS collaboration, PRL107 (2011) 052302



- In 2011, CMS collaboration observed disappearance of 2S and 3S upsilon state in Pb-Pb collisions
- sequential suppression

Why lattice NRQCD?



- M.Cheng et al, (Columbia-BNL-RBC-Bielefeld) PRD 77 (2008) 014511, $N_f = 2 + 1$, $m_{\pi} = 220$ MeV
- strongly interacting QGP and absence of scale symmetry

• Thermodynamic QCD can be investigated using

$$\langle O \rangle = \frac{\text{Tr}Oe^{-\beta H}}{\text{Tr}e^{-\beta H}} \rightarrow \frac{\int D\phi Oe^{-\int d^{4}x \pounds_{E}}}{\int D\phi e^{-\int d^{4}x \pounds_{E}}}$$
(1)

• Lattice QCD allows systematic study of non-perturbative physics using first principles of quantum field theory by numerically evaluating this integral

• Lattice QCD is defined on discrete space-time lattices

 \rightarrow various scales $(a_{\tau}, N_s a_s, N_{\tau} a_{\tau} = \frac{1}{T}, \frac{1}{M_q})$

- Temperature can be changed by changing *a* (by changing lattice coupling) or N_τ
- Note that $a_{ au} << rac{1}{M_a}$ and $N_{ extsf{s}} a_{ extsf{s}} \gtrsim$ typical hadron size

• For the bottom quark, it is difficult to satisfy this condition with the current state of computing powers

 \rightarrow simulate effective field theory, NRQCD

• bottomon quark velocity $v = \frac{p}{M}$ is small (non-relativistic) in the bottomonium rest frame and momentum scale $> M_q$ is "integrated away" (Bodwin et al, PRD51 (1995) 1125)

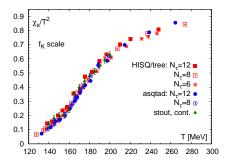
• Foldy-Wouthuysen-Tani transform gives non-relativistic QCD lagrangian from QCD lagrangian

$$\mathcal{L}_{q} = \psi^{\dagger} \left(D_{t} - \frac{\mathbf{D}^{2}}{2M_{q}} \right) \psi + \mathcal{O}(v^{4})$$
(1)

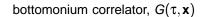
• gauge field ensemble has thermal effect and bottom quark moves under this background gauge field

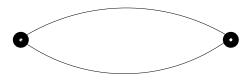
• construct bottomonium correlators out of NRQCD bottom quark correlator

• gauge field in thermal environment is from HotQCD (PRD85 (2012) 054503)



strange quark number susceptibility ($m_l = 0.05 m_s$)





• NRQCD dispersion relation has undetermined zero point energy

$$E_q = \sqrt{M_q^2 + \mathbf{p}^2} \sim M_q + \frac{\mathbf{p}^2}{2M_q} - \frac{\mathbf{p}^4}{8M_q^3} + \cdots$$
 (1)

• simulation at zero temperature is required to determine the zero point energy

- consistent lattice NRQCD requires $M_q a_\tau \sim 1$
- To keep NRQCD as an effective field theory remain valid, $T \ll M_q$
- In summary, a consistent lattice NRQCD for bottomonium $(M_b = 4.65 \text{ GeV})$ requires

$$a_{\tau}\gtrsim\frac{1}{4.65}(\text{GeV}^{-1}) \tag{1}$$

and

$$T = \frac{1}{N_{\tau}a_{\tau}} \le \frac{4.65 \text{GeV}^{-1}}{N_{\tau}} \tag{2}$$

• If we are interested in a few MeV temperature, $N_{\tau} \sim O(10)$

spectral function in NRQCD

In QCD,

$$\begin{aligned} \mathcal{F}_{\Gamma}(\tau) &= \sum_{\vec{x}} \langle \overline{\psi}(\tau, \vec{x}) \Gamma \psi(\tau, \vec{x}) \overline{\psi}(0, \vec{0}) \Gamma \psi(0, \vec{0}) \rangle \\ &= \int \frac{d^3 p}{(2\pi)^3} \int_0^\infty \frac{d\omega}{2\pi} \mathcal{K}(\tau, \omega) \rho_{\Gamma}(\omega, \vec{p}) \end{aligned} \tag{3}$$

and

$$K(\tau,\omega) = \frac{\cosh[\omega(\tau - 1/2T)]}{\sinh(\omega/2T)}.$$
(5)

• the spectral function of Euclidean correlator has all the information on the finite temperature behavior of a propagator

- numerically ill-posed problem
- Maximum Entropy Method is used (cf. M. Asakawa, T. Hatsuda, Y. Nakahara, PPNP46 (2001) 459)

spectral function in NRQCD

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and

$$K(\tau,\omega) = \frac{\cosh[\omega(\tau - 1/2T)]}{\sinh(\omega/2T)}.$$
(5)

• known to have problems (cf. T. Umeda, PRD75 (2007) 094502 and A. Mocsy and P. Petreczky, PRD77 (2008) 014501)

• both the kernel($K(\tau, \omega)$) and the spectral density($\rho_{\Gamma}(\omega, \vec{p})$) depend on temperature

constant contribution

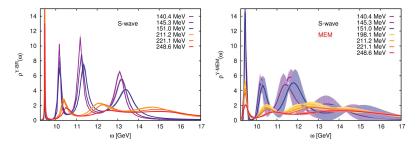
spectral function in NRQCD

• In NRQCD, with $\omega=2\textit{M}+\omega'$ and $\textit{T}/\textit{M}<<1,\,\textit{K}(\tau,\omega)\rightarrow e^{-\omega\tau}$

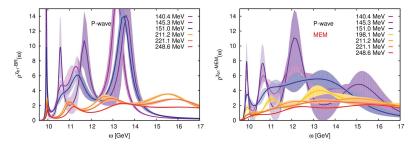
$$G(\tau) = \int_{-2M}^{\infty} \frac{d\omega'}{2\pi} \exp(-\omega'\tau)\rho(\omega')$$
(3)

- inverse Laplace transform problem
- new improved Bayesian method (Burnier-Rothkopf, PRL111 (2013) 182003, next talk)

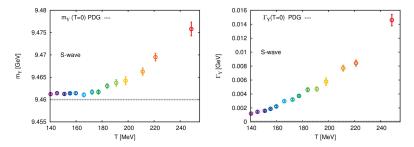
Υ channel spectral function



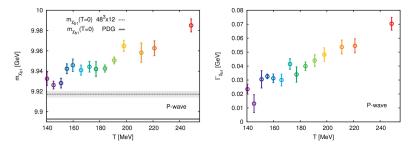
χ_{b1} channel spectral function



temperature dependence of $\Upsilon(1S)$ mass and it width



temperature dependence of $\chi_{b1}(1P)$ mass and it width



Conclusion

• On T = 0 and $T \neq 0$, lattice NRQCD + new Baysesian Reconstruction (BR) of spectral function on bottomonium, which is systematically improvable and is based on the first principel of quantum field theory (not a model)

• free from known problem in QCD (constant contribution problem) and improvement from MEM

• from both BR and MEM, the ground state of Υ survives but the excited states are suppressed as the temperature increases above T_c

• 1S peak of Υ channell starts to increase at $T\gtrsim$ 1.14 T_c and its width increases monotonically in T

• From BR, the ground state of χ_{b1} retains peak structure even at 1.6 T_c but from MEM, χ_b (P-wave) melts around 1.3 T_c